Syeda Reeha Quasar

14114802719

4C7

Aim

To implement following sorting techniques and analyze their time complexity.

Experiment - 1

Algorithms Design and Analysis Lab

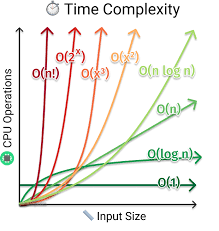
# **EXPERIMENT – 1**

## **Aim:**

To implement following sorting techniques and analyze their time complexity.

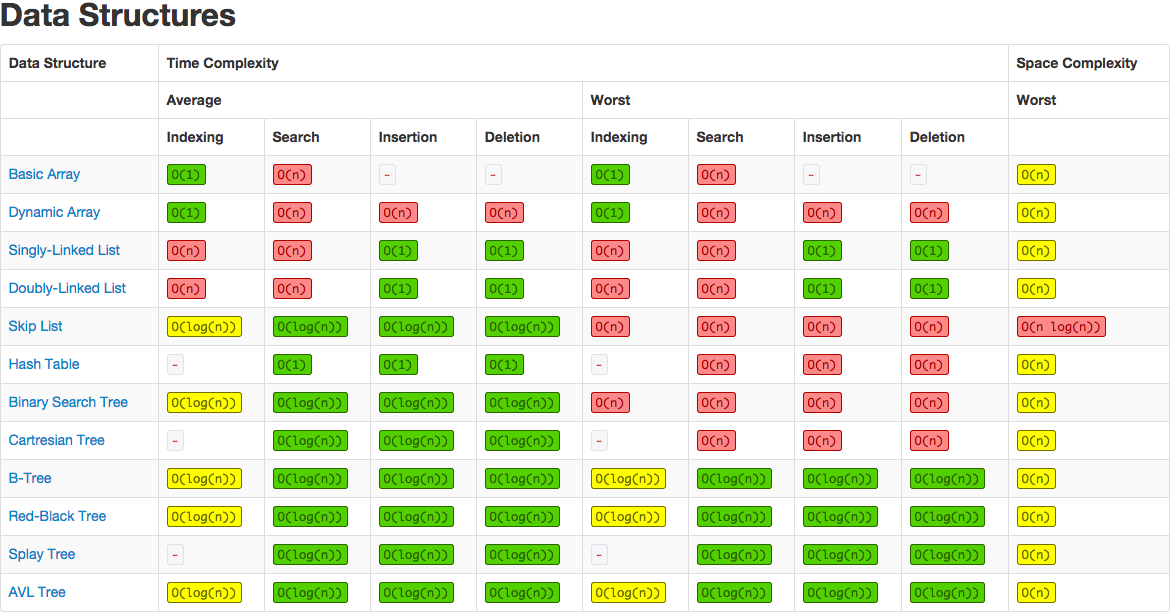
## **Theory:**

**Time complexity** is the amount of time taken by an algorithm to run, as a function of the length of the input. It measures the time taken to execute each statement of code in an algorithm.



Data Structure with their Time Complexity:

Legend



# Clock/time analysis implementation

#### **Code**

#include <iostream>

#include <ctime>

using namespace std;

int main() {

  // use time() with NULL argument

  //   cout << time(NULL);

  time\_t current\_time;

  // stores time in current\_time

  time(&current\_time);

  cout << current\_time;

  cout << " seconds has passed since 00:00:00 GMT, Jan 1, 1970";

  return 0;

}

#### **Output**

# 

# Sorting implementation

#### **Code**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void printArray(int arr[], int size) {

int i;

for (i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main() {

int arr[] = {64, 34, 25, 12, 22, 11, 90};

int n = sizeof(arr)/sizeof(arr[0]);

auto start = chrono::steady\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

cout << "Array: ";

printArray(arr, n);

cout << endl;

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

auto end = chrono::steady\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

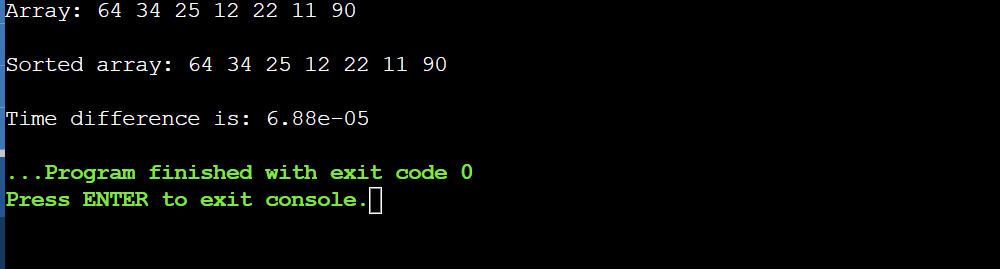
time\_taken \*= 1e-9;

cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

#### **Output**



## **1.1 Bubble Sort:**

This sorting algorithm is comparison-based algorithm in which each pair of adjacent elements is compared, and the elements are swapped if they are not in order.

### **Pseudo code**

**We assume list is an array of n elements. We further assume that swap function swaps the values of the given array elements.**

***begin BubbleSort (list)***

***for all elements of list***

***if list[i] > list[i+1]***

***swap (list[i], list [i+1])***

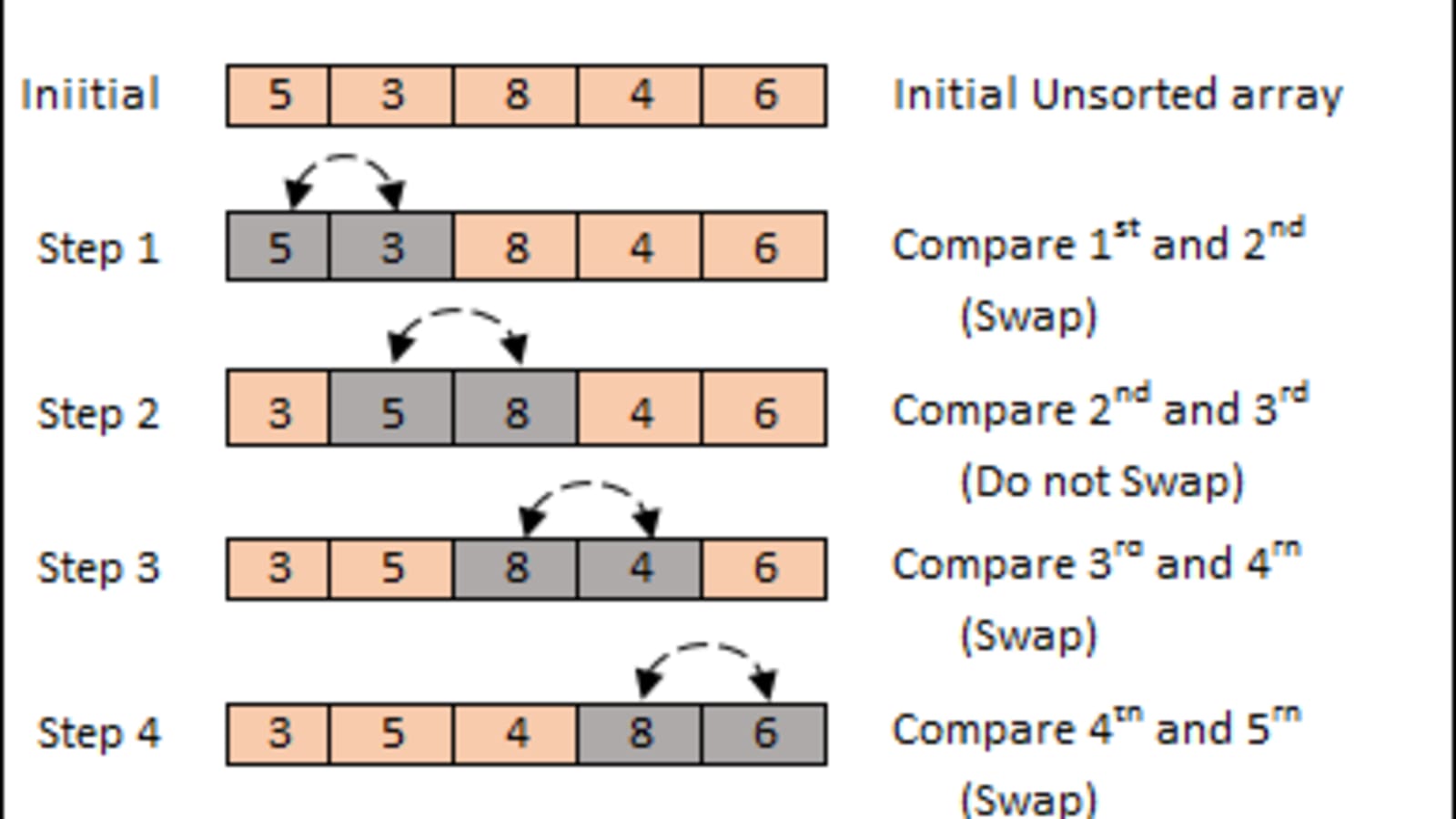
***end if***

***end for***

***return list***

***end BubbleSort***

### **Example:**



### **Result and Analysis**

Worst and Average Case Time Complexity: O (n\*n). Worst case occurs when array is reverse sorted and its time complexity is O (n\*n) and Best case occurs when array is already sorted and its time complexity is O (n) (linear time). This sort takes just O (1) extra space.

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void swap(int \*xp, int \*yp) {

int temp = \*xp;

\*xp = \*yp;

\*yp = temp;

}

void bubbleSort(int arr[], int n) {

int i, j;

bool swapped;

for (i = 0; i < n - 1; i++) {

swapped = false;

for (j = 0; j < n - i - 1; j++) {

if (arr[j] > arr[j+1]) {

swap(&arr[j], &arr[j + 1]);

swapped = true;

}

}

if (swapped == false) {// no swap means array sorted so break out

break;

}

}

}

void printArray(int arr[], int size) {

int i;

for (i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main() {

// int arr[] = {64, 34, 25, 12, 22, 11, 90};

// int n = sizeof(arr)/sizeof(arr[0]);

int n = rand() % 100;

int arr[n];

for (int i = 0; i < n; i++) {

arr[i] = rand() % 100;

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

bubbleSort(arr, n);

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

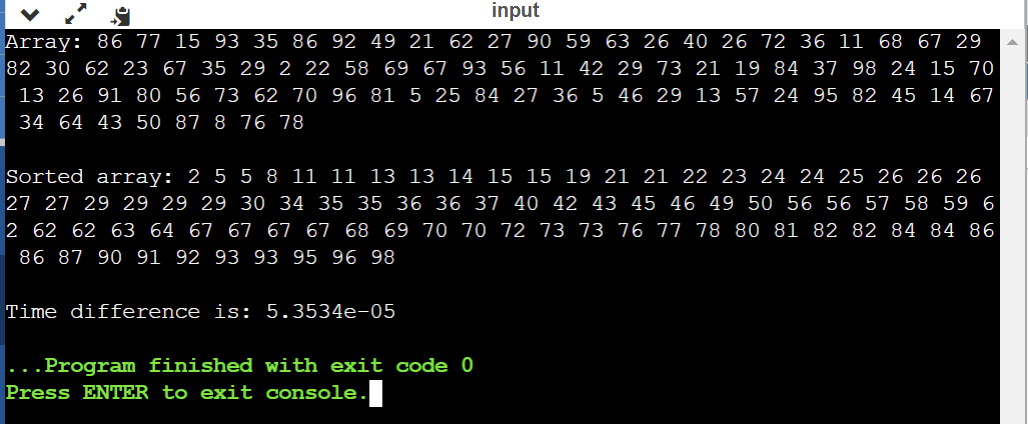
time\_taken \*= 1e-9;

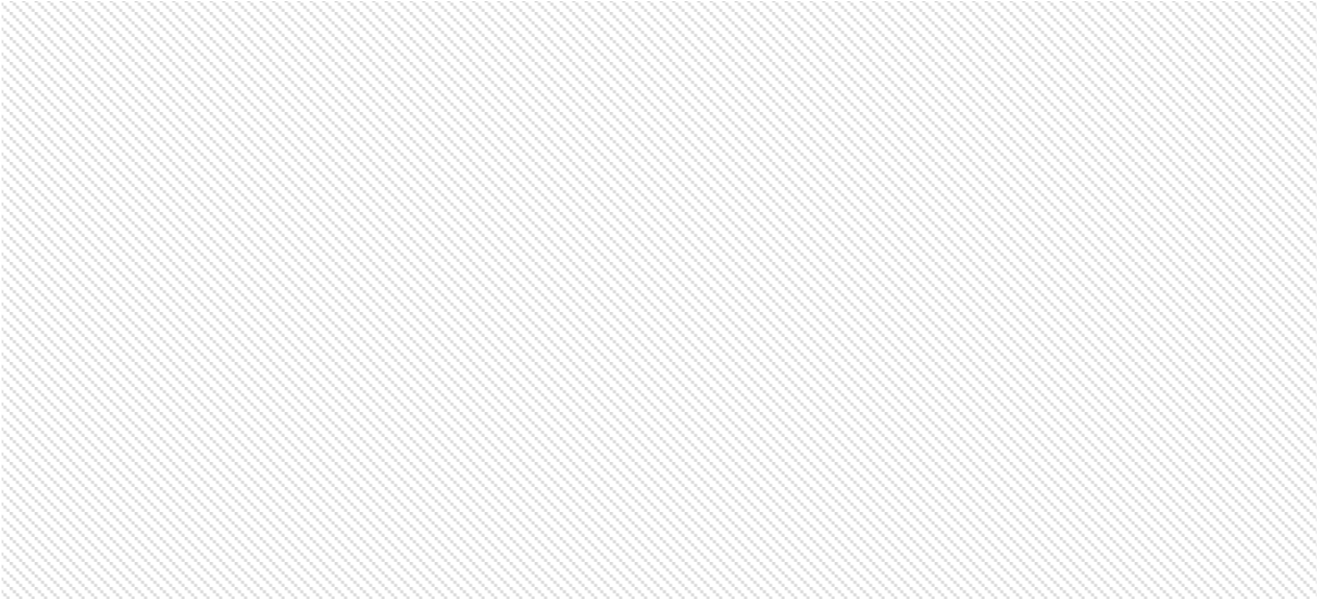
cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

**Output:**





-1

0

1

2

3

4

5

6

7

8

9

0

10000

20000

30000

40000

50000

60000

**Bubble Sort**

time(best)

time (avg)

time(worst)

# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void swap(int \*xp, int \*yp)

{

int temp = \*xp;

\*xp = \*yp;

\*yp = temp;

}

void bubbleSort(int arr[], int n)

{

int i, j;

bool swapped;

for (i = 0; i < n - 1; i++)

{

swapped = false;

for (j = 0; j < n - i - 1; j++)

{

if (arr[j] > arr[j + 1])

{

swap(&arr[j], &arr[j + 1]);

swapped = true;

}

}

if (swapped == false)

{ // no swap means array sorted so break out

break;

}

}

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

double sortApp(int n)

{

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

auto start = chrono::high\_resolution\_clock::now();

ios\_base::sync\_with\_stdio(false);

bubbleSort(arr, n);

auto end = chrono::high\_resolution\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

return time\_taken;

}

int main()

{

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

times[x] = sortApp(n);

}

cout << "value of n's: " << endl;

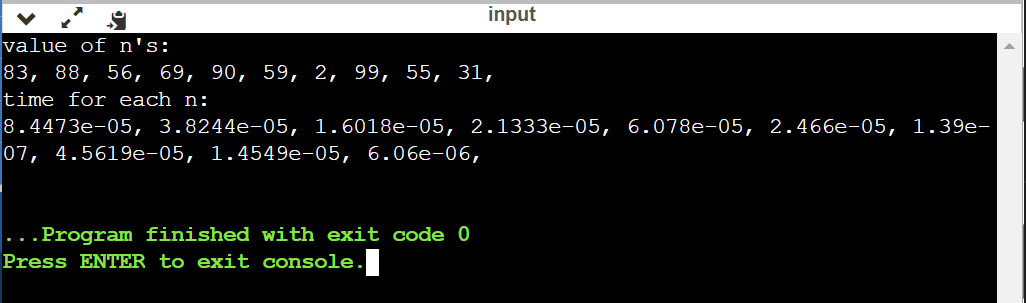
printArray(ns, 10);

cout << "time for each n: " << endl;

printArray(times, 10);

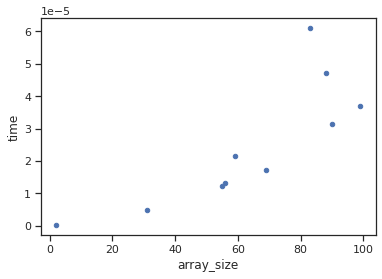
}

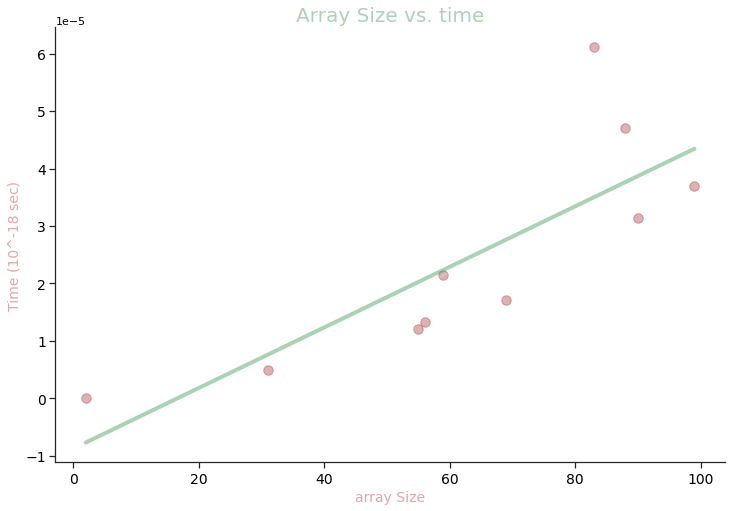
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [6.1129e-05, 4.7125e-05, 1.3298e-05, 1.7092e-05, 3.147e-05, 2.1538e-05, 8.6e-08, 3.6987e-05, 1.2126e-05, 4.909e-06]**

****

****

# **Bubble Sort**

# **Viva Questions**

### **1. How can the best-case efficiency of bubble sort be improved?**

### Ans.

Some iterations can be skipped if the list is sorted, hence efficiency improves to O(n).

A better version of bubble sort, known as modified bubble sort, includes a flag that is set if an exchange is made after an entire pass over the array. If no exchange is made, then it should be clear that the array is already in order because no two elements need to be switched.

### **2. Is bubble sorting a stable sort?**

Ans.

**Yes**

sorting algorithm is said to be stable if two objects with equal keys appear in the same order in sorted output as they appear in the input array to be sorted.

### **3. How much time will bubble sort take if all the elements are same?**

Ans.

O(n)

Bubble sort has a worst-case and average complexity of О(n2), where n is the number of items being sorted. Most practical sorting algorithms have substantially better worst-case or average complexity, often O(n log n).

### **4. What would happen if bubble sort didn’t keep track of the number of swaps made on each pass through the list?**

Ans.

**The algorithm wouldn't know when to terminate as it would have no way of** knowing when the list was in sorted order.

### **5. List main properties to be considered in bubble sort?**

Ans.

* Large values are always sorted first.
* It only takes one iteration to detect that a collection is already sorted.
* The best time complexity for Bubble Sort is O(n). ...
* The space complexity for Bubble Sort is O(1), because only single additional memory space is required.

## **1.2 Bucket Sort:**

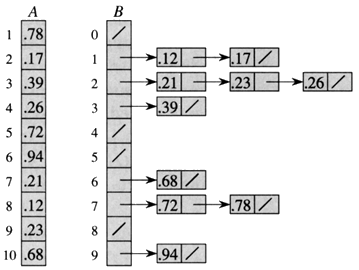
**Bucket sort**, or **bin sort**, is a sorting algorithm that works by distributing the elements of an array into a number of buckets. Each bucket is then sorted individually, either using a different sorting algorithm, or by recursively applying the bucket sorting algorithm.

It is a distribution sort, a generalization of pigeonhole sort, and is a cousin of radix sort in the most-to-least significant digit flavour. Bucket sort can be implemented with comparisons and therefore can also be considered a comparison sort algorithm.

It works as follows:

1. Set up an array of initially empty "buckets".
2. **Scatter**: Go over the original array, putting each object in its bucket.
3. Sort each non-empty bucket.
4. **Gather**: Visit the buckets in order and put all elements back into the original array.

. This will be the sorted list.



### **Pseudo code**

**The code assumes that input is an n-element array A and each element in A satisfies 0 ≤ *A*[*i*] ≤ 1. We also need an auxiliary array B [0 . . *n*-1] for linked-lists (buckets).**

***BUCKET SORT (A)***

***1. n ← length [A]***

***2. For i =1 to n do***

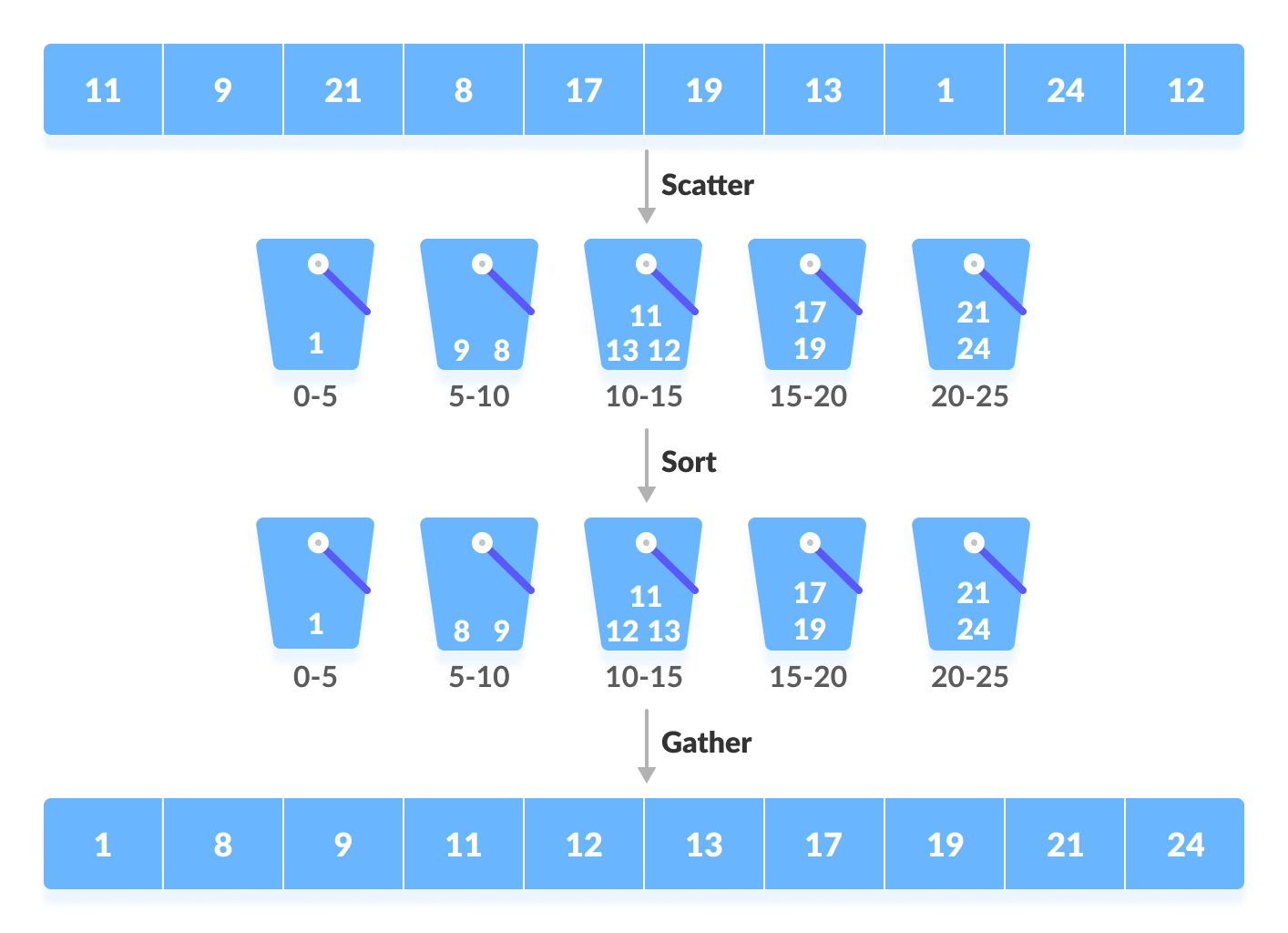
***3. Insert A[i]into list B [A[i]/b] where b is the bucket size***

***4. For i =0 to n-1do***

***5. Sort list B with Insertion sort***

***6. Concatenate the lists B [0], B [1] ... B [n-1] together in order.***

### **Example:**



### **Result and Analysis**

In the above Bucket sort algorithm, we observe in the *best case*, the algorithm distributes the elements uniformly between buckets, a few elements are placed on each bucket and sorting the buckets is **O (1)**. Rearranging the elements is one more run through the initial list.

T (n) = [time to insert *n* elements in array *A*] + [time to go through auxiliary array *B* [0 . . . *n*-1] \* (Sort by INSERTION\_SORT)  
       = O (*n*) + (*n*-1) (*n*)  
       = O (*n*)

In the *worst case*, the elements are sent all to the same bucket, making the process take **O (n^2)**.

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void bucketSort(float arr[], int n) {

vector<float> bucket[n];

// put elemets in respective buckets

for (int i = 0; i < n; i++) {

int bi = n \* arr[i]; // Index in bucket

bucket[bi].push\_back(arr[i]);

}

for (int i = 0; i < n; i++) // sorting each buckets

sort(bucket[i].begin(), bucket[i].end());

int index = 0;

for (int i = 0; i < n; i++) // Concatenate all buckets into arr[]

for (int j = 0; j < bucket[i].size(); j++)

arr[index++] = bucket[i][j];

}

void printArray(float arr[], int size) {

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main() {

// int arr[] = {64, 34, 25, 12, 22, 11, 90};

// int n = sizeof(arr)/sizeof(arr[0]);

int n = rand() % 100;

float arr[n];

for (int i = 0; i < n; i++) {

arr[i] = (float(rand())/float((RAND\_MAX)));

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

bucketSort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

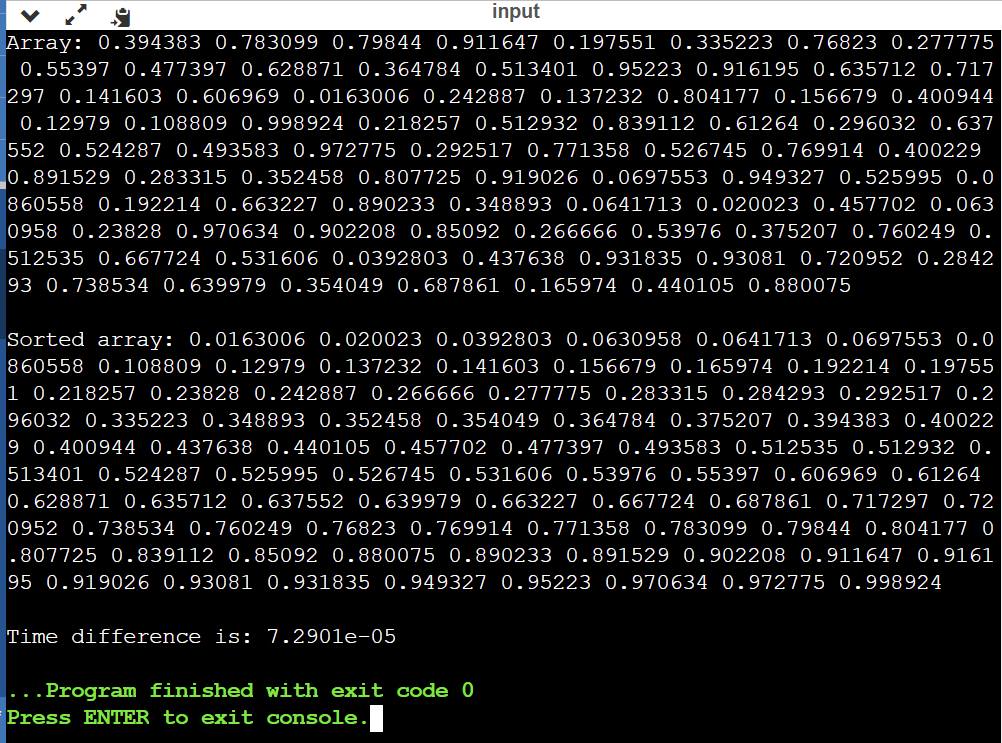
time\_taken \*= 1e-9;

cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

**Output:**



# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void bucketSort(float arr[], int n)

{

vector<float> bucket[n];

// put elemets in respective buckets

for (int i = 0; i < n; i++)

{

int bi = n \* arr[i]; // Index in bucket

bucket[bi].push\_back(arr[i]);

}

for (int i = 0; i < n; i++) // sorting each buckets

sort(bucket[i].begin(), bucket[i].end());

int index = 0;

for (int i = 0; i < n; i++) // Concatenate all buckets into arr[]

for (int j = 0; j < bucket[i].size(); j++)

arr[index++] = bucket[i][j];

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main()

{

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

float arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = (float(rand()) / float((RAND\_MAX)));

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

bucketSort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

// printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

times[x] = time\_taken;

cout << "Time difference is: " << time\_taken << setprecision(6) << endl;

}

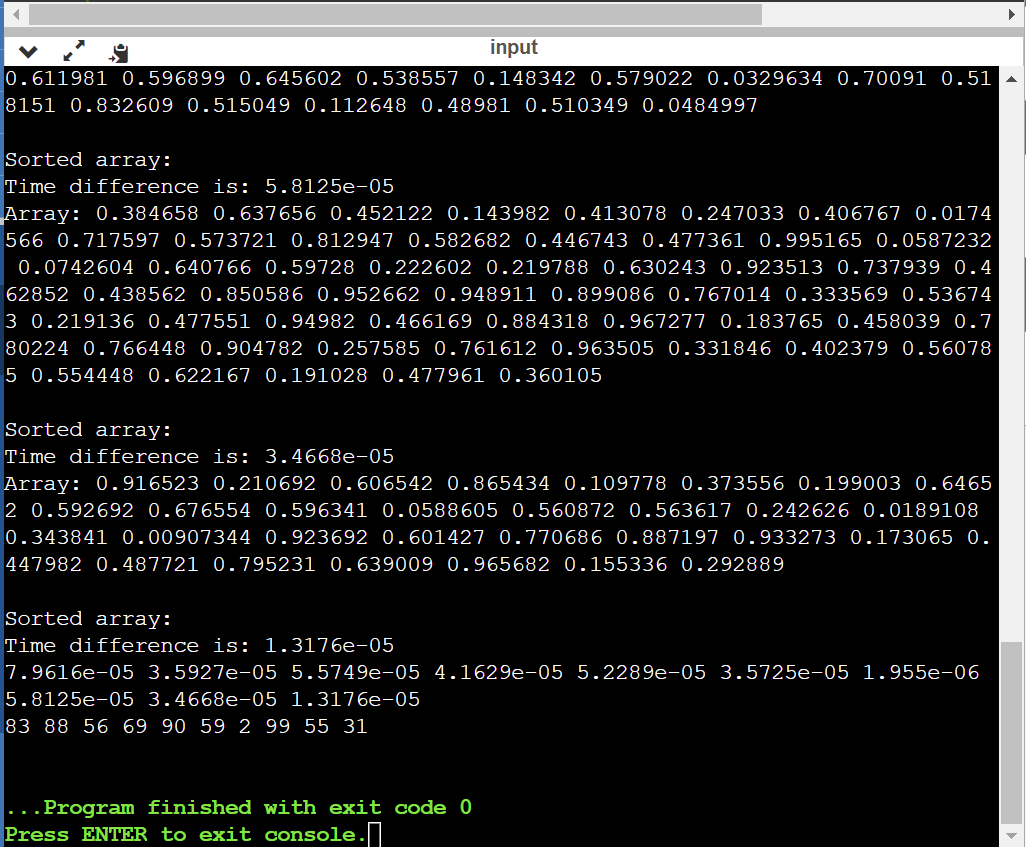
printArray(times, 10);

printArray(ns, 10);

return 0;

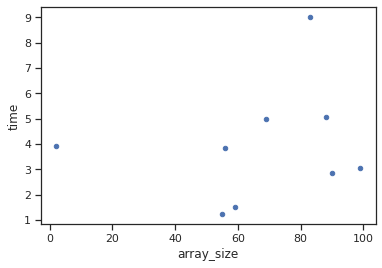
}

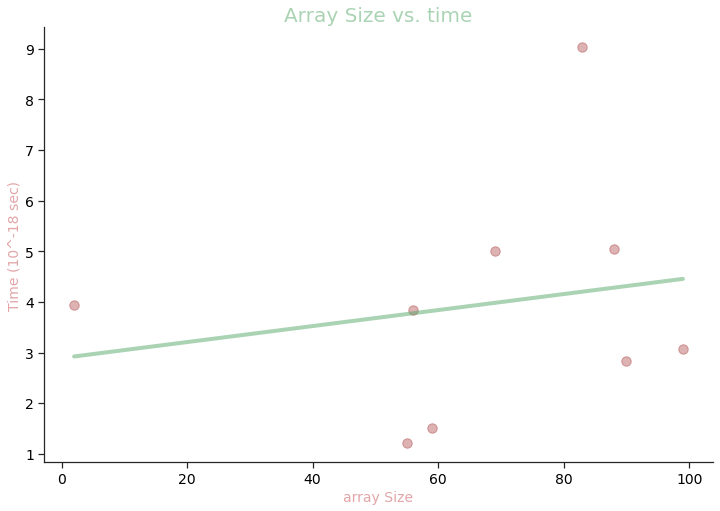
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [9.0298, 5.0532, 3.8491, 5.0068, 2.8416, 1.505, 3.9323, 3.0733, 1.2236]**

****

**Bucket Sort**

# **Viva Questions**

### **1. Is the bucket sort in place sort? Why or why not?**

### Ans.

**No, it's not an in-place sorting algorithm**. The whole idea is that input sorts themselves as they are moved to the buckets.

### **2. Is bucket sort a stable sort?**

Ans.

Bucket sort is stable, if the underlying sort is also stable, as equal keys are inserted in order to each bucket. Counting sort works by determining how many integers are behind each integer in the input array A. Using this information, the input integer can be directly placed in the output array B.

### **3. Why bucket sort is good for large size arrays?**

Ans.

Yes

The advantage of bucket sort is **that once the elements are distributed into buckets, each bucket can be processed independently of the others**. This means that you often need to sort much smaller arrays as a follow-up step than the original array.  
Bucket sort works by distributing the array elements into a number of buckets. So bucket sort is most efficient in the case **when the input is uniformly distributed**.

### **4. State any disadvantage of using this sort.**

Ans.

1. The problem is that if the buckets are distributed incorrectly, you may wind up spending a lot of extra effort for no or very little gain. As a result, bucket sort works best when the data is more or less evenly distributed, or when there is a smart technique to pick the buckets given a fast set of heuristics based on the input array.
2. Can’t apply it to all data types since a suitable bucketing technique is required. Bucket sort’s efficiency is dependent on the distribution of the input values, thus it’s not worth it if your data are closely grouped.In many situations, you might achieve greater performance by using a specialized sorting algorithm like radix sort, counting sort, or burst sort instead of bucket sort.
3. Bucket sort’s performance is determined by the number of buckets used, which may need some additional performance adjustment when compared to other algorithms.

### **5. Can this sort be used for sorting negative numbers?**

Ans.

Using Bucket sort for negative values simply **requires mapping each element to a bucket proportional to its** a distance from the minimal value to be sorted.

**sortMixed(arr[], n)**

1) Split array into two parts

create two Empty vector Neg[], Pos[]

(for negative and positive element respectively)

Store all negative element in Neg[] by converting

into positive (Neg[i] = -1 \* Arr[i] )

Store all +ve in pos[] (pos[i] = Arr[i])

2) Call function bucketSortPositive(Pos, pos.size())

Call function bucketSortPositive(Neg, Neg.size())

**bucketSortPositive(arr[], n)**

3) Create n empty buckets (Or lists).

4) Do following for every array element arr[i].

a) Insert arr[i] into bucket[n\*array[i]]

5) Sort individual buckets using insertion sort.

6) Concatenate all sorted buckets.

## **1.3 Radix Sort:**

### Radix Sort is a non-comparative sorting algorithm. It is one of the most efficient and fastest linear sorting algorithms. In radix sort, we first sort the elements based on last digit (least significant digit). Then the result is again sorted by second digit, continue this process for all digits until we reach most significant digit. We use counting sort to sort elements of every digit.

### **Pseudo code**

***Radix-Sort(A, d)***

***//It works same as counting sort for d number of passes.***

***//Each key in A [1...n] is a d-digit integer.***

***// (Digits are numbered 1 to d from right to left.)***

***for j = 1 to d do***

***//A[]-- Initial Array to Sort***

***intcount[10] = {0};***

***//Store the count of "keys" in count[]***

***//key- it is number at digit place j***

***for i = 0 to n do***

***count[key of(A[i]) in pass j]++***

***fork = 1 to 10 do***

***count[k] = count[k] + count[k-1]***

***//Build the resulting array by checking***

***//new position of A[i] from count[k]***

***for i = n-1 down to 0 do***

***result[ count[key of(A[i])] ] = A[j]***

***count[key of(A[i])]--***

***//Now main array A[] contains sorted numbers***

***//according to current digit place***

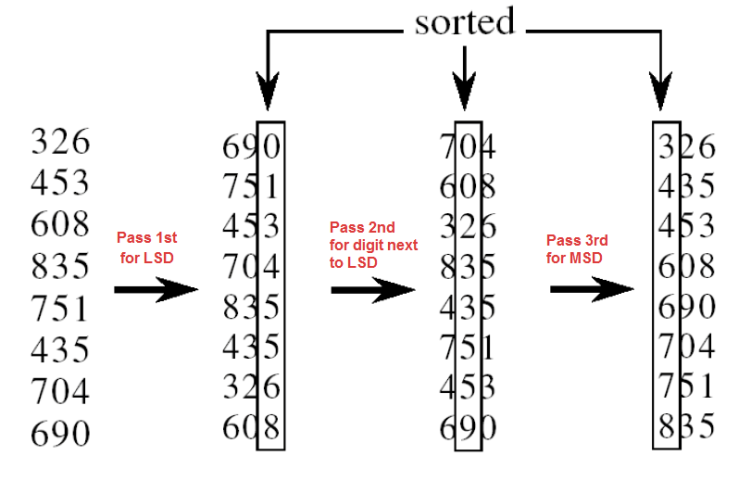
***for i=0 to n do***

***A[i] = result[i]***

***end for(j)***

***end func***

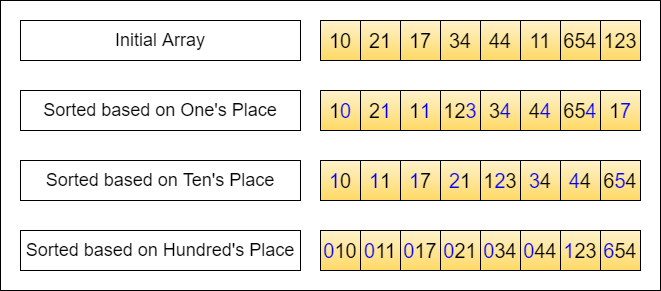
### **Example:**



In the above example:  
**For 1st pass:** We sort the array on basis of least significant digit (1s place) using counting sort. Notice that 435 is below 835, because 435 occurred below 835 in the original list.  
**For 2nd pass:** We sort the array on basis of next digit (10s place) using counting sort. Notice that here 608 is below 704, because 608 occurred below 704 in the previous list, and similarly for (835, 435) and (751, 453).  
**For 3rd pass:** We sort the array on basis of most significant digit (100s place) using counting sort. Notice that here 435 is below 453, because 435 occurred below 453 in the previous list, and similarly for (608, 690) and (704, 751).

### **Result and Analysis**

In this algorithm running time depends on intermediate sorting algorithm which is counting sort. If the range of digits is from 1 to k, then counting sort time complexity is O (n+k). There are d passes i.e. counting sort is called d time, so total time complexity is O (nd+nk) =O (nd). As k=O (n) and d is constant, so radix sort runs in linear time. It performs the same way for best case as well



**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

int getMax(int arr[], int n) {

int maxEle = arr[0];

for (int i = 1; i < n; i++)

if (arr[i] > maxEle)

maxEle = arr[i];

return maxEle;

}

void countSort(int arr[], int n, int exp) {

int output[n]; // output array

int count[10] = { 0 };

// Store count of occurrences in count[]

for (int i = 0; i < n; i++)

count[(arr[i] / exp) % 10]++;

// Change count[i] so that count[i] now contains actual position of this digit in output[]

for (int i = 1; i < 10; i++)

count[i] += count[i - 1];

for (int i = n - 1; i >= 0; i--) {

output[count[(arr[i] / exp) % 10] - 1] = arr[i];

count[(arr[i] / exp) % 10]--;

}

// Copy the output array to arr[], so that arr[] now contains sorted numbers according to current digit

for (int i = 0; i < n; i++)

arr[i] = output[i];

}

void radixsort(int arr[], int n) {

// Find the maximum number to know number of digits

int m = getMax(arr, n);

// Do counting sort for every digit. Note that instead of passing digit number, exp is passed. exp is 10^i where i is current digit number

for (int exp = 1; m / exp > 0; exp \*= 10)

countSort(arr, n, exp);

}

void printArray(int arr[], int size) {

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main() {

// int arr[] = {64, 34, 25, 12, 22, 11, 90};

// int n = sizeof(arr)/sizeof(arr[0]);

int n = rand() % 100;

int arr[n];

for (int i = 0; i < n; i++) {

arr[i] = rand() % 100;

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

radixsort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

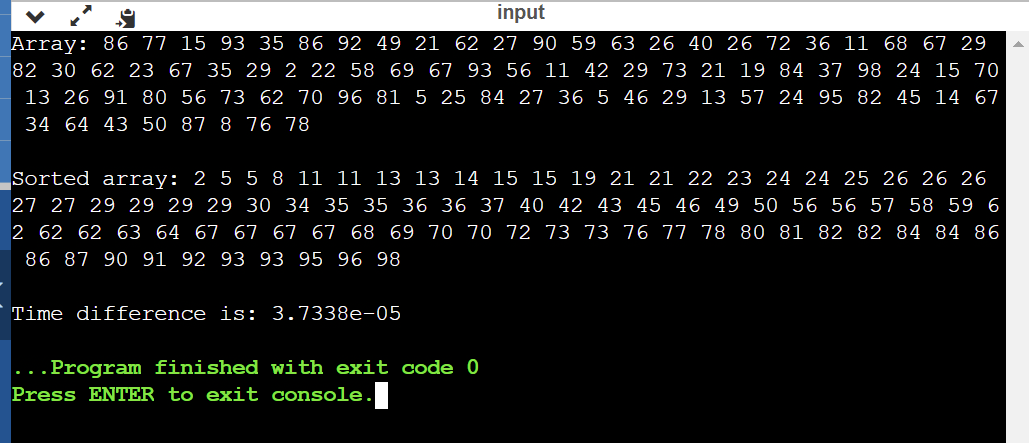
time\_taken \*= 1e-9;

cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

**Output:**



# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

int getMax(int arr[], int n) {

int maxEle = arr[0];

for (int i = 1; i < n; i++)

if (arr[i] > maxEle)

maxEle = arr[i];

return maxEle;

}

void countSort(int arr[], int n, int exp) {

int output[n]; // output array

int count[10] = { 0 };

// Store count of occurrences in count[]

for (int i = 0; i < n; i++)

count[(arr[i] / exp) % 10]++;

// Change count[i] so that count[i] now contains actual position of this digit in output[]

for (int i = 1; i < 10; i++)

count[i] += count[i - 1];

for (int i = n - 1; i >= 0; i--) {

output[count[(arr[i] / exp) % 10] - 1] = arr[i];

count[(arr[i] / exp) % 10]--;

}

// Copy the output array to arr[], so that arr[] now contains sorted numbers according to current digit

for (int i = 0; i < n; i++)

arr[i] = output[i];

}

void radixsort(int arr[], int n) {

// Find the maximum number to know number of digits

int m = getMax(arr, n);

// Do counting sort for every digit. Note that instead of passing digit number, exp is passed. exp is 10^i where i is current digit number

for (int exp = 1; m / exp > 0; exp \*= 10)

countSort(arr, n, exp);

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

double sortApp(int n) {

int arr[n];

for (int i = 0; i < n; i++) {

arr[i] = rand() % 100;

}

auto start = chrono::high\_resolution\_clock::now();

ios\_base::sync\_with\_stdio(false);

radixsort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

return time\_taken;

}

int main() {

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

times[x] = sortApp(n);

}

cout << "value of n's: " << endl;

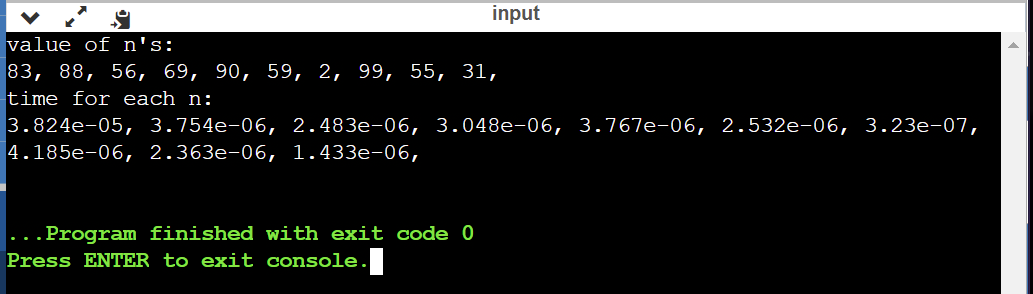
printArray(ns, 10);

cout << "time for each n: " << endl;

printArray(times, 10);

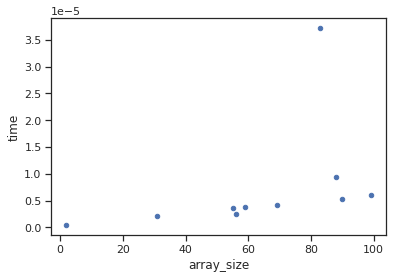
}

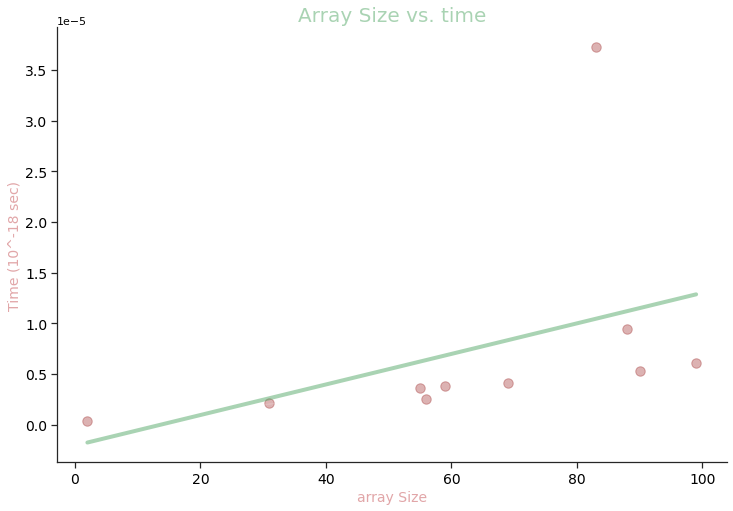
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [3.7257e-05, 9.437e-06, 2.511e-06, 4.097e-06, 5.246e-06, 3.785e-06, 3.63e-07, 6.097e-06, 3.63e-06, 2.104e-06]**

****

**Radix Sort**

# **Viva Questions**

### **1. Is Radix Sort preferable to Comparison based sorting algorithms like Quick-Sort?**

### Ans. If we have log2n bits for every digit, the **running time of Radix appears to be better than Quick Sort** for a wide range of input numbers. The constant factors hidden in asymptotic notation are higher for Radix Sort and Quick-Sort uses hardware caches more effectively.

Radix sort is slower for (most) real world use cases.

One reason is the complexity of the algorithm:

If items are unique, k >= log(n). Even with duplicate items, the set of problems where k < log(n) is small.

Another is the implementation:

The additional memory requirement (which in it self is a disadvantage), affects cache performance negatively.

### **2. Is this sort stable?**

Ans.

No

MSD sorts are not necessarily stable if the original ordering of duplicate keys must always be maintained. Other than the traversal order, MSD and LSD sorts differ in their handling of variable length input. LSD sorts can group by length, radix sort each group, then concatenate the groups in size order.

### **3. How much additional space is taken by this sort?**

Ans.

O(k + n)

Radix sort's **space complexity is bound to the sort it uses to sort each radix**. In best case, that is counting sort. As you can see, counting sort creates multiple arrays, one based on the size of K, and one based on the size of N. B is the output array which is size n.

### **4. State any disadvantage of using this sort?**

Ans.

* Since Radix Sort depends on digits or letters, Radix Sort is much less flexible than other sorts. Hence , for every different type of data it needs to be rewritten.
* The constant for Radix sort is greater compared to other sorting algorithms.
* It takes more space compared to Quicksort which is inplace sorting.

### **5. How can the performance of this sort be improved?**

Ans.

Bucket sort is mainly useful when input is uniformly distributed over a range. For example, consider the following problem.   
*Sort a large set of floating point numbers which are in range from 0.0 to 1.0 and are uniformly distributed across the range. How do we sort the numbers efficiently?*  
A simple way is to apply a comparison based sorting algorithm. The [lower bound for Comparison based sorting algorithm](https://www.geeksforgeeks.org/lower-bound-on-comparison-based-sorting-algorithms/) (Merge Sort, Heap Sort, Quick-Sort .. etc) is Ω(n Log n), i.e., they cannot do better than nLogn.   
Can we sort the array in linear time? [Counting sort](https://www.geeksforgeeks.org/counting-sort/) can not be applied here as we use keys as index in counting sort. Here keys are floating point numbers.    
The idea is to use bucket sort.

## **1.4 Shell Sort:**

Itis a generalized version of insertion sort. It is an in–place comparison sort. It is also known as **diminishing increment sort**; it is one of the oldest sorting algorithms invented by Donald L. Shell (1959.)This algorithm uses insertion sort on the large interval of elements to sort. Then the interval of sorting keeps on decreasing in a sequence until the interval reaches 1. These intervals are known as **gap sequence.**

Increment Sequences:

Shell’s original sequence: N/2 , N/4 , …, 1 (repeatedly divide by 2);

Hibbard’s increments: 1, 3, 7, …, 2k – 1 ;

Knuth’s increments: 1, 4, 13, …, (3k – 1) / 2 ;

Sedge wick’s increments: 1, 5, 19, 41, 109…

Here interval is calculated based on Knuth's formula as −

Knuth's Formula

h = h \* 3 + 1, where ->h is interval with initial value 1

**Pseudo code**

***Procedure shellSort ()***

***A: array of items***

***/\* calculate interval\*/***

***while interval < A. length /3 do:***

***interval = interval \* 3 + 1***

***end while***

***while interval > 0 do:***

***for outer = interval; outer < A. length; outer ++ do:***

***/\* select value to be inserted \*/***

***ValueToInsert = A[outer]***

***inner = outer;***

***/\*shift element towards right\*/***

***while inner > interval -1 &&A [inner - interval] >= valueToInsert do:***

***A[inner] = A [inner - interval]***

***inner = inner - interval***

***end while***

***/\* insert the number at hole position \*/***

***A[inner] = valueToInsert***

***end for***

***/\* calculate interval\*/***

***interval = (interval -1) /3;***

***end while***

***end procedure***

### **Example:**

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | ***a*1** | ***a*2** | ***a*3** | ***a*4** | ***a*5** | ***a*6** | ***a*7** | ***a*8** | ***a*9** | ***a*10** | ***a*11** | ***a*12** |
| **Input data** | 62 | 83 | 18 | 53 | 07 | 17 | 95 | 86 | 47 | 69 | 25 | 28 |
| **After 5-sorting** | 17 | 28 | 18 | 47 | 07 | 25 | 83 | 86 | 53 | 69 | 62 | 95 |
| **After 3-sorting** | 17 | 07 | 18 | 47 | 28 | 25 | 69 | 62 | 53 | 83 | 86 | 95 |
| **After 1-sorting** | 07 | 17 | 18 | 25 | 28 | 47 | 53 | 62 | 69 | 83 | 86 | 95 |

The first pass, 5-sorting, performs insertion sort on five separate sub arrays (*a*1, *a*6, *a*11 ), (*a*2, *a*7, *a*12), (*a*3, *a*8), (*a*4, *a*9), (*a*5, *a*10). For instance, it changes the sub array (*a*1, *a*6, *a*11) from (62, 17, 25) to (17, 25, 62). The next pass, 3-sorting, performs insertion sort on the three sub arrays (*a*1, *a*4, *a*7, *a*10), (*a*2, *a*5, *a*8, *a*11), (*a*3, *a*6, *a*9, *a*12). The last pass, 1-sorting, is an ordinary insertion sort of the entire array (*a*1... *a*12).

### **Result and Analysis**

Since in this algorithm insertion sort is applied in the large interval of elements and then interval reduces in a sequence, therefore the running time of Shell sort is heavily dependent on the gap sequence it uses. So in worst case time complexity is  *O (n2)* and in Average Case time complexity depends on gap sequence while in Best Case Time complexity is O(n\*log n)

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

int shellSort(int arr[], int n) {

    for (int gap = n/2; gap > 0; gap /= 2)  {

        for (int i = gap; i < n; i += 1)    {

            int temp = arr[i];

            // shift gap sorted elements to find position for ith element

            int j = i;

            for (j; j >= gap && arr[j - gap] > temp; j -= gap)

                arr[j] = arr[j - gap];

            arr[j] = temp; // place i th element in correct position

        }

    }

    return 0;

}

void printArray(int arr[], int size)    {

    for (int i = 0; i < size; i++)

        cout << arr[i] << " ";

    cout << endl;

}

int main()  {

    // int arr[] = {64, 34, 25, 12, 22, 11, 90};

    // int n = sizeof(arr)/sizeof(arr[0]);

    int n = rand() % 100;

    int arr[n];

    for (int i = 0; i < n; i++) {

        arr[i] = rand() % 100;

    }

    cout << "Array: ";

    printArray(arr, n);

    cout << endl;

    auto start = chrono::high\_resolution\_clock::now();

    // unsync the I/O of C and C++.

    ios\_base::sync\_with\_stdio(false);

    shellSort(arr, n);  // sort arr

    auto end = chrono::high\_resolution\_clock::now();

    cout << "Sorted array: ";

    printArray(arr, n);

    cout << endl;

    double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

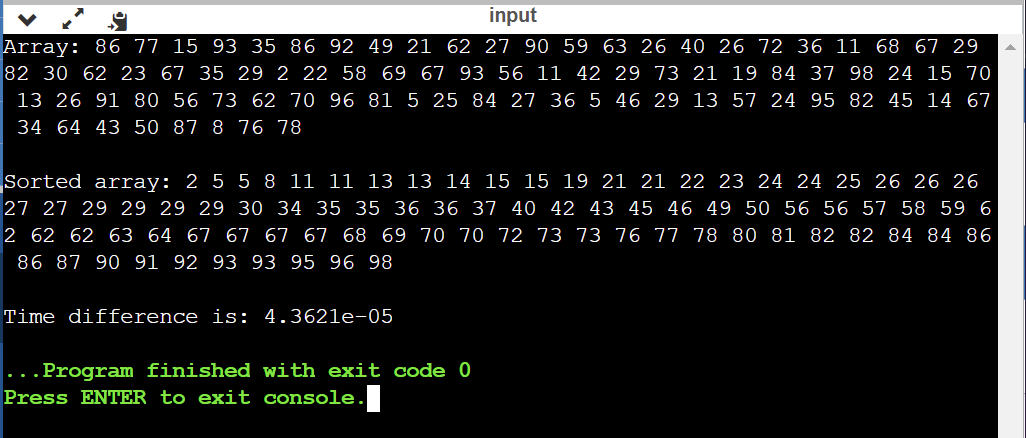
    time\_taken \*= 1e-9;

    cout << "Time difference is: " << time\_taken << setprecision(6);

    return 0;

}

**Output:**



# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

int shellSort(int arr[], int n) {

for (int gap = n/2; gap > 0; gap /= 2) {

for (int i = gap; i < n; i += 1) {

int temp = arr[i];

// shift gap sorted elements to find position for ith element

int j = i;

for (j; j >= gap && arr[j - gap] > temp; j -= gap)

arr[j] = arr[j - gap];

arr[j] = temp; // place i th element in correct position

}

}

return 0;

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

double sortApp(int n) {

int arr[n];

for (int i = 0; i < n; i++) {

arr[i] = rand() % 100;

}

auto start = chrono::high\_resolution\_clock::now();

ios\_base::sync\_with\_stdio(false);

shellSort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

return time\_taken;

}

int main() {

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

times[x] = sortApp(n);

}

cout << "value of n's: " << endl;

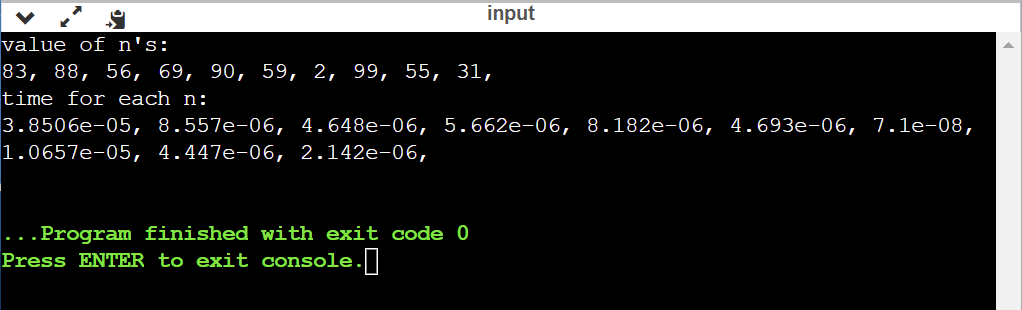
printArray(ns, 10);

cout << "time for each n: " << endl;

printArray(times, 10);

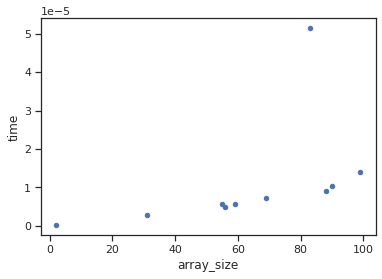
}

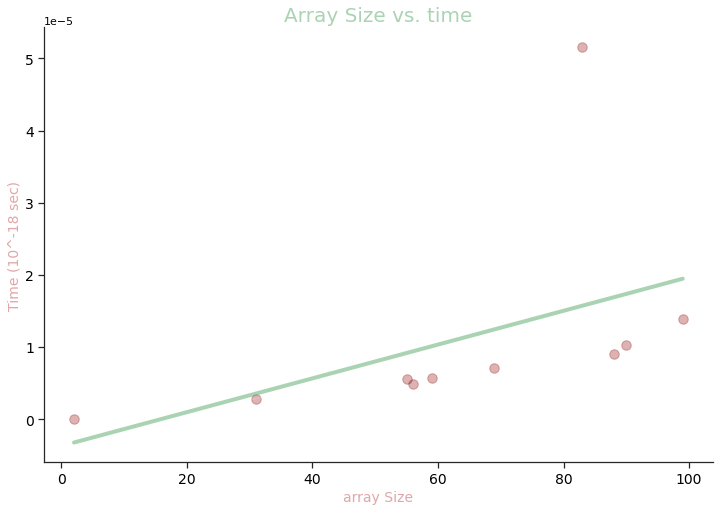
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [5.1556e-05, 9.109e-06, 4.9e-06, 7.176e-06, 1.0281e-05, 5.658e-06, 9e-08, 1.3916e-05, 5.566e-06, 2.774e-06]**

****

****

**Shell Sort**

# **Viva Questions**

### **1. How can the time complexity of shell sort be improved?**

### Ans.

Shell Sort improves its time complexity by taking the advantage of the fact that using Insertion Sort on a partially sorted array results in less number of moves.

### **2. State any application of shell sort?**

Ans.

* Shellsort performs more operations and has higher cache miss ratio than quicksort.
* However, since it can be implemented using little code and does not use the call stack, some implementations of the qsort function in the C standard library targeted at embedded systems use it instead of quicksort. Shellsort is, for example, used in the uClibc library. For similar reasons, an implementation of Shellsort is present in the Linux kernel.
* Shellsort can also serve as a sub-algorithm of introspective sort, to sort short subarrays and to prevent a slowdown when the recursion depth exceeds a given limit. This principle is employed, for instance, in the bzip2 compressor.

### **3. Given the following list of numbers: [5,16,20,12,3,8,9,17,19,7]. What is the content of the list after all swapping is complete for a gap size of 3?**

Ans.

[5, 3, 8, 7, 16, 19, 9, 17, 20, 12]

### **4. Is this sort stable and does it takes extra additional space?**

Ans.

Yes, Shell sort is a stable Algorithm.

No, No addition space is required. Shell sort is an in-place sorting algorithm as it requires **O(1)** auxiliary space.

## **1.5 Selection Sort:**

Selection sort is a simple sorting algorithm. This sorting algorithm is an in-place comparison-based algorithm in which the list is divided into two parts, the sorted part at the left end and the unsorted part at the right end. Initially, the sorted part is empty and the unsorted part is the entire list. The smallest element is selected from the unsorted array and swapped with the leftmost element, and that element becomes a part of the sorted array. This process continues moving unsorted array boundary by one element to the right.

The selection sort algorithm sorts an array by repeatedly finding the minimum element (considering ascending order) from unsorted part and putting it at the beginning. The algorithm maintains two subarrays in a given array.

1) The subarray which is already sorted.   
2) Remaining subarray which is unsorted.

**Pseudo code**

***Procedure selection sort***

***list: array of items***

***n: size of list***

***for i = 1 to n - 1***

***/\* set current element as minimum\*/***

***min = i***

***/\* check the element to be minimum \*/***

***for j = i+1 to n***

***if list[j] < list [min] then***

***min = j;***

***end if***

***end for***

***/\* swap the minimum element with the current element\*/***

***if indexMin != i then***

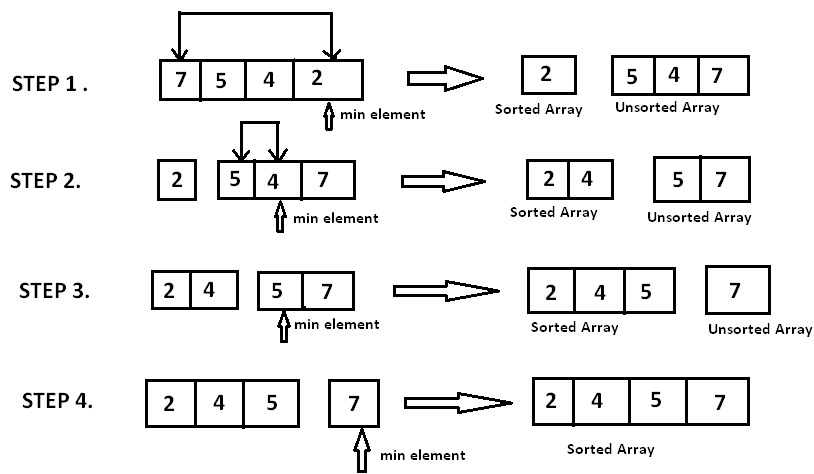
***swap list[min] and list[i]***

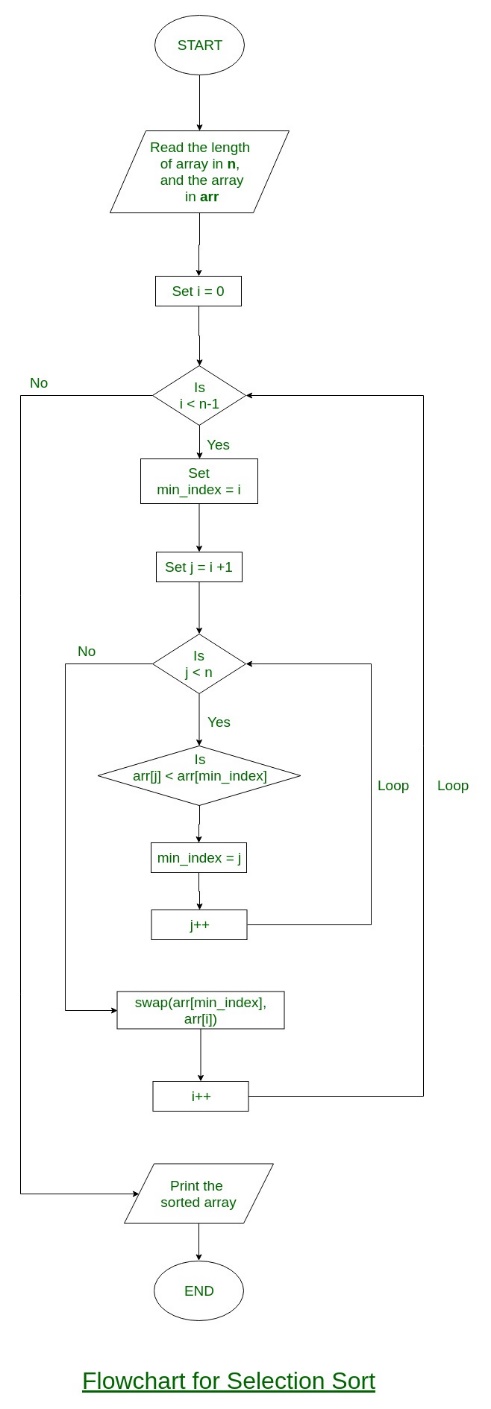
***end if***

***end for***

***end procedure:***

### **Example:**





### **Result and Analysis**

To find the minimum element from the array of N elements, N−1 comparisons are required. After putting the minimum element in its proper position, the size of an unsorted array reduces to N−1 and then N−2 comparisons are required to find the minimum in the unsorted array. Therefore (N−1) + (N−2) + ....... + 1 = (N (N−1))/2 comparisons and N swaps result in the overall complexity of O (N2

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void swap(int \*xp, int \*yp)

{

int temp = \*xp;

\*xp = \*yp;

\*yp = temp;

}

// keep finding minimum element and place it in beginning

void selectionSort(int arr[], int n)

{

for (int i = 0; i < n - 1; i++)

{

int min\_idx = i;

for (int j = i + 1; j < n; j++)

if (arr[j] < arr[min\_idx])

min\_idx = j;

swap(&arr[min\_idx], &arr[i]); // swap min with first

}

}

void printArray(int arr[], int size)

{

int i;

for (i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main()

{

// int arr[] = {64, 34, 25, 12, 22, 11, 90};

// int n = sizeof(arr)/sizeof(arr[0]);

int n = rand() % 100;

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

selectionSort(arr, n);

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

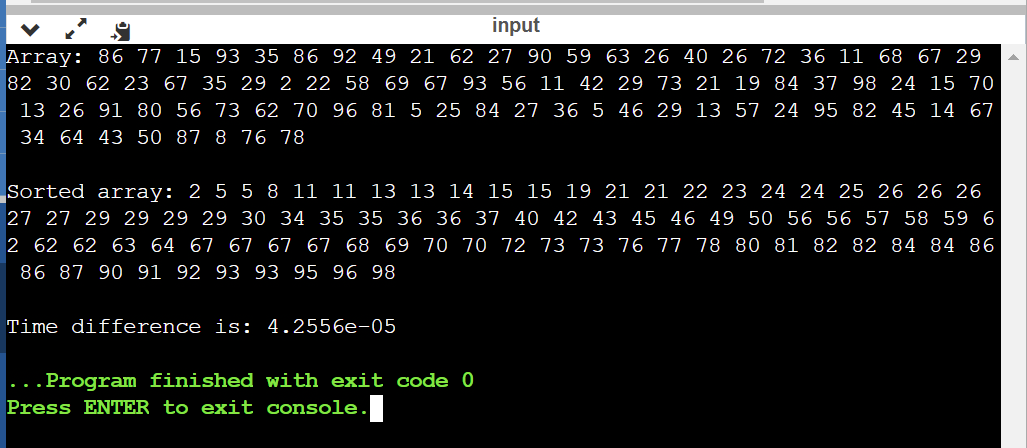
time\_taken \*= 1e-9;

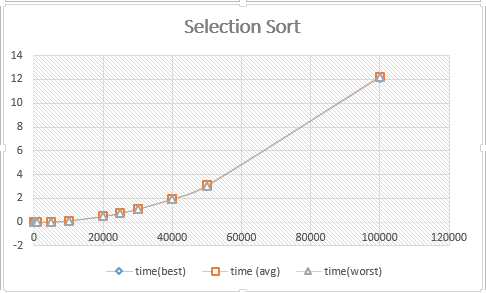
cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

**Output:**





# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void swap(int \*xp, int \*yp)

{

int temp = \*xp;

\*xp = \*yp;

\*yp = temp;

}

// keep finding minimum element and place it in beginning

void selectionSort(int arr[], int n)

{

for (int i = 0; i < n - 1; i++)

{

int min\_idx = i;

for (int j = i + 1; j < n; j++)

if (arr[j] < arr[min\_idx])

min\_idx = j;

swap(&arr[min\_idx], &arr[i]); // swap min with first

}

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

double sortApp(int n)

{

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

auto start = chrono::high\_resolution\_clock::now();

ios\_base::sync\_with\_stdio(false);

selectionSort(arr, n);

auto end = chrono::high\_resolution\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

return time\_taken;

}

int main()

{

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

times[x] = sortApp(n);

}

cout << "value of n's: " << endl;

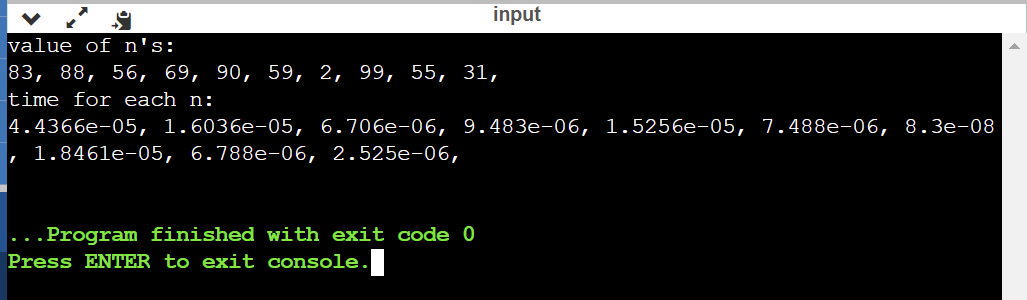
printArray(ns, 10);

cout << "time for each n: " << endl;

printArray(times, 10);

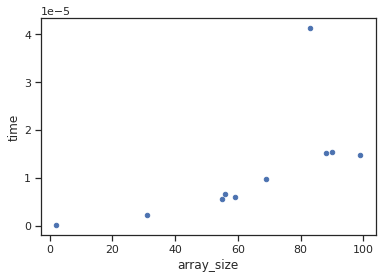
}

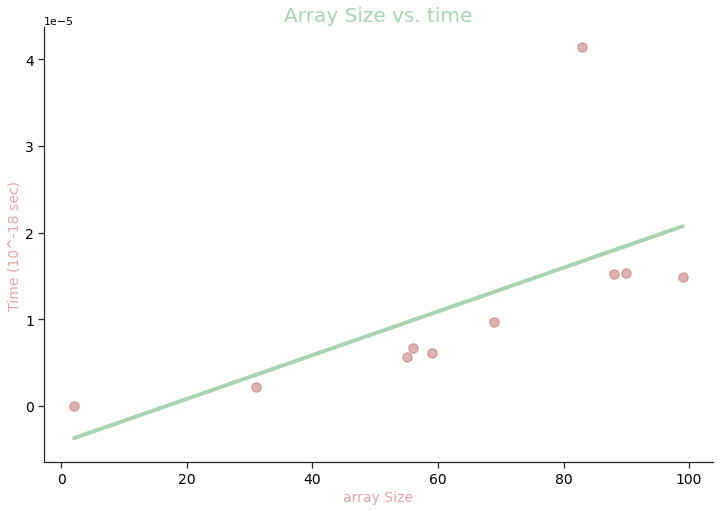
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [4.1399e-05, 1.5271e-05, 6.697e-06, 9.652e-06, 1.537e-05, 6.069e-06, 4.2e-08, 1.4875e-05, 5.673e-06, 2.172e-06]**

****

****

**Selection Sort**

# **Viva Questions**

### **1. What is the average case performance of Selection Sort?**

### Ans.

**Θ(N2)**

Average Case Time Complexity is: **O(N2)**

### **2. For each i from 1 to n-1, how many comparisons are there in this sort?**

Ans.

Selection sort finds the smallest element and swaps it into the first position. The, from the remaining N-1 elements after the first one (which we know is the smallest), it finds the next smallest and swaps it into the 2nd position. And so on.

To find the smallest element from a group of N elements takes N-1 comparisons. Basically, compare item 1 to 2, remember the smallest. Compare item 3 to smallest and remember which ever is smaller, and so on. You end up doing 1 comparison for every element from 2 through N.

We have to find the smallest element N-1 times\*, but each time we have a smaller list to look through.

For N elements it takes 1+2+3+…+N-1 = (N-1)N/2 comparisons.

### **3. If all the input elements are identical then how it will affect the time taken by this sort?**

Ans.

Selection sort will run in **O(n^2)** regardless of whether the array is already sorted or not.

### **4. What is the output of selection sort after the 2nd iteration given the following sequence of numbers: 16 3 46 9 28 14**

Ans.

3 9 46 16 28 14

### **5. What is straight selection sort?**

Ans.

Selection sorting refers to a class of algorithms for sorting a list of items using comparisons. These algorithms select successively smaller or larger items from the list and add them to the output sequence. This is an improvement of the Simple Selection Sort and it is called Straight Selection Sort. Therefore, instead of replacing the selected element by a unique value in the i-th pass (as happens in Simple Selection Sort), the selected element is exchanged with the i-th element.

## **1.6 Heap Sort:**

This algorithm is divided into two basic parts:

* Creating a Heap of the unsorted list.
* Then a sorted array is created by repeatedly removing the largest/smallest element from the heap, and inserting it into the array. The heap is reconstructed after each removal.

**What is a heap?**

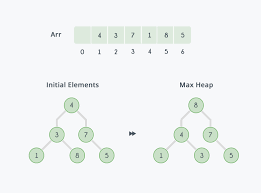
Heap is a special tree-based data structure, which satisfies the following special heap properties:

**Shape Property:** Heap data structure is always a Complete Binary Tree, which means all levels of the tree are fully filled.

**Heap Property:** All nodes are either *[greater than or equal to]* or *[less than or equal to]* each of its children. If the parent nodes are greater than their children, heap is called a **Max-Heap**, and if the parent nodes are smaller than their child nodes, heap is called **Min-Heap**.

Initially on receiving an unsorted list, the first step in heap sort is to create a Heap data structure (Max-Heap or Min-Heap). Once heap is built, the first element of the Heap is either largest or smallest (depending upon Max-Heap or Min-Heap), so we put the first element of the heap in our array. Then we again make heap using the remaining elements, to again pick the first element of the heap and put it into the array. We keep on doing the same repeatedly until we have the complete sorted list in our array.

Heap sort is a comparison-based sorting technique based on Binary Heap data structure. It is similar to selection sort where we first find the minimum element and place the minimum element at the beginning. We repeat the same process for the remaining elements.



### **Pseudo code**

***Heapsort (A) {***

***BuildHeap(A)***

***for i <- length (A) downto 2 {***

***exchange A [1] <-> A[i]***

***heapsize <- heapsize -1***

***Heapify(A, 1)***

***}***

***BuildHeap (A) {***

***heapsize <- length (A)***

***for i <- floor (length/2) downto 1***

***Heapify (A, i)***

***}***

***Heapify (A, i) {***

***le <- left (i)***

***ri <- right(i)***

***if (le<=heapsize) and (A[le]>A[i])***

***largest <- le***

***else***

***largest <- i***

***if (ri<=heapsize) and (A[ri]>A[largest])***

***largest <- ri***

***if (largest != i) {***

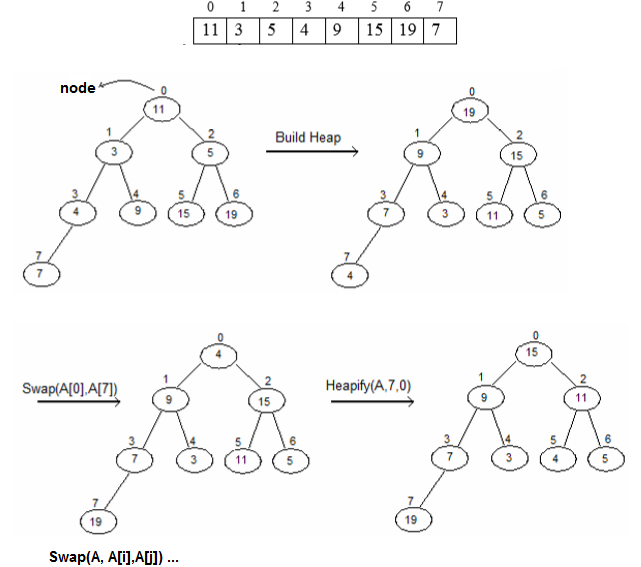
***exchange A[i] <-> A[largest]***

***Heapify(A, largest)***

***}***

***}***

### **Example:**



### **Result and Analysis**

Heap sort has the best possible worst case running time complexity of O (n Log n).It doesn't need any extra storage and that makes it good for situations where array size is large. Heapify runs in time O (h) and there are at most n=2h+1-1 nodes in an almost complete binary tree of height h, so Heapify runs in time O (ln n). Build-Heap calls Heapify n/2 times, so it takes O (n h) = O (n ln n).

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void heapify(int arr[], int n, int root)

{

int largest = root;

int leftChild = 2 \* root + 1;

int rightChild = 2 \* root + 2;

if (leftChild < n && arr[leftChild] > arr[largest])

largest = leftChild;

if (rightChild < n && arr[rightChild] > arr[largest])

largest = rightChild;

if (largest != root)

{

swap(arr[root], arr[largest]);

heapify(arr, n, largest);

}

}

void heapSort(int arr[], int n)

{

// Build heap

for (int i = n / 2 - 1; i >= 0; i--)

heapify(arr, n, i);

for (int i = n - 1; i > 0; i--)

{ // ectract elements from heap

swap(arr[0], arr[i]); // Move current root to end

heapify(arr, i, 0); // call max heapify on the reduced heap

}

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main()

{

// int arr[] = {64, 34, 25, 12, 22, 11, 90};

// int n = sizeof(arr)/sizeof(arr[0]);

int n = rand() % 100;

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

heapSort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

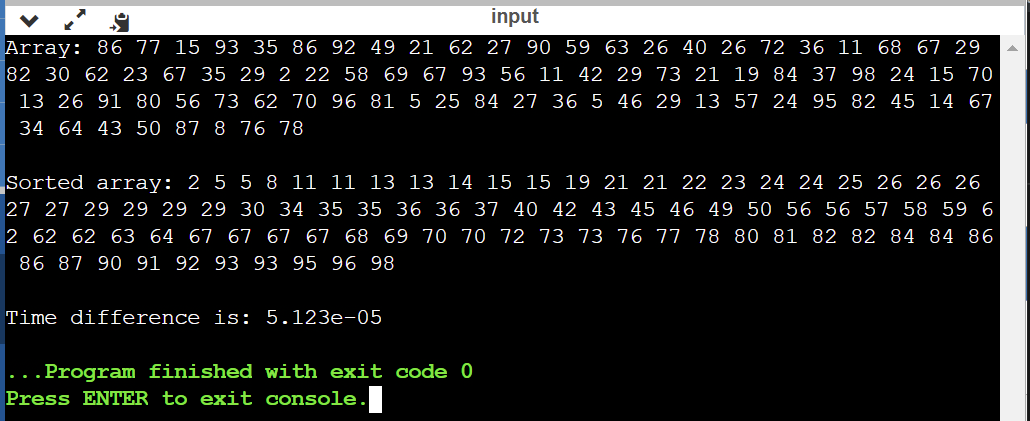
time\_taken \*= 1e-9;

cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

**Output:**



# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

void heapify(int arr[], int n, int root)

{

int largest = root;

int leftChild = 2 \* root + 1;

int rightChild = 2 \* root + 2;

if (leftChild < n && arr[leftChild] > arr[largest])

largest = leftChild;

if (rightChild < n && arr[rightChild] > arr[largest])

largest = rightChild;

if (largest != root)

{

swap(arr[root], arr[largest]);

heapify(arr, n, largest);

}

}

void heapSort(int arr[], int n)

{

// Build heap

for (int i = n / 2 - 1; i >= 0; i--)

heapify(arr, n, i);

for (int i = n - 1; i > 0; i--)

{ // ectract elements from heap

swap(arr[0], arr[i]); // Move current root to end

heapify(arr, i, 0); // call max heapify on the reduced heap

}

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

double sortApp(int n)

{

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

auto start = chrono::high\_resolution\_clock::now();

ios\_base::sync\_with\_stdio(false);

heapSort(arr, n); // sort arr

auto end = chrono::high\_resolution\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

return time\_taken;

}

int main()

{

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

times[x] = sortApp(n);

}

cout << "value of n's: " << endl;

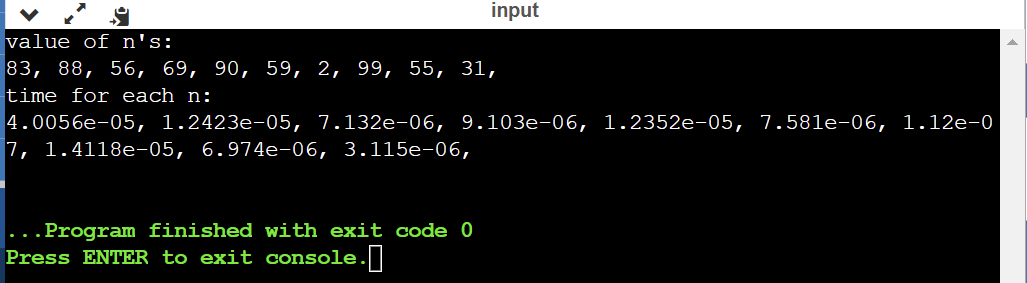
printArray(ns, 10);

cout << "time for each n: " << endl;

printArray(times, 10);

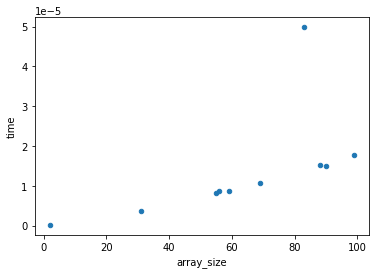
}

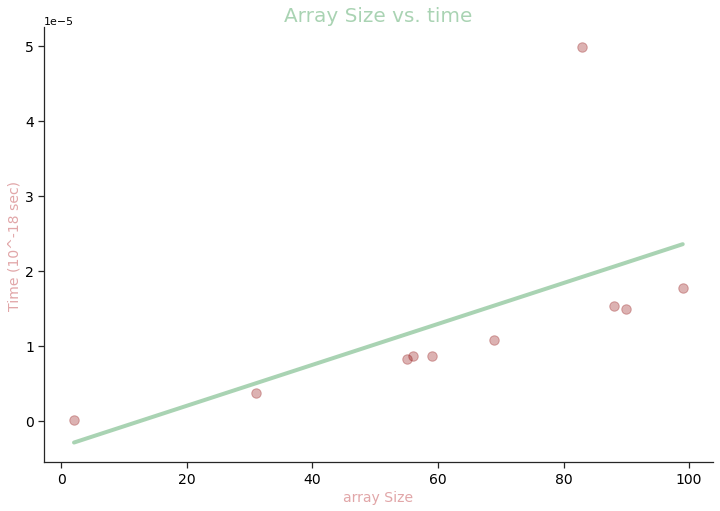
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [4.9828e-05, 1.5332e-05, 8.655e-06, 1.0828e-05, 1.4977e-05, 8.714e-06, 1.48e-07, 1.7703e-05, 8.224e-06, 3.716e-06]**

****

**Heap Sort**

# **Viva Questions**

### **1. What are the minimum and maximum numbers of elements in a heap of height *h*?**

### Ans.

2h

A heap of height h is complete up to the level at depth h−1and needs to have at least one node on level h.

Therefore the minimum total number of nodes must be at least ∑h−1i=02i+1=2h−1+1=2h.∑i=0h−12i+1=2h−1+1=2h., and this tight since an heap with 2h nodes has height h.

### **2. Where in a heap might the smallest element reside?**

Ans.

**Smallest element will be at the last level of the max heap.**

### **3. Is an array that is in reverse sorted order a heap?**

Ans.

The correct version of this statement is "An array sorted in ascending order is can be treated **as min- heap**" and its complementry statement is "An array sorted in descending order can be treated as max heap"

### **4. Does heap sort uses extra space for storage?**

Ans.

 No, The Heap sort algorithm can be implemented as an in-place sorting algorithm. This means that its memory usage is minimal because apart from what is necessary to hold the initial list of items to be sorted, it needs no additional memory space to work.

### **5. What is the effect of calling HEAPIFY *(A, i*) when the element A[*i*] is larger than its children?**

Ans.

No effect. The comparisons are carried out, A[i]A[i] is found to be largest and the procedure just returns.

## **1.7 Insertion Sort:**

Insertion sort is a simple sorting algorithm that works similar to the way you sort playing cards in your hands. The array is virtually split into a sorted and an unsorted part. Values from the unsorted part are picked and placed at the correct position in the sorted part.

**Algorithm**   
To sort an array of size n in ascending order:   
1: Iterate from arr[1] to arr[n] over the array.   
2: Compare the current element (key) to its predecessor.   
3: If the key element is smaller than its predecessor, compare it to the elements before. Move the greater elements one position up to make space for the swapped element.

### **Example:**



### **Result and Analysis**

**Time Complexity:** O(n^2)   
**Auxiliary Space:**O(1)  
**Boundary Cases**: Insertion sort takes maximum time to sort if elements are sorted in reverse order. And it takes minimum time (Order of n) when elements are already sorted.  
**Algorithmic Paradigm:** Incremental Approach  
**Sorting In Place:** Yes  
**Stable:** Yes  
**Online:** Yes  
**Uses:** Insertion sort is used when number of elements is small. It can also be useful when input array is almost sorted, only few elements are misplaced in complete big array.

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

// place current element in right order as we move forward

void insertionSort(int arr[], int n)

{

for (int i = 1; i < n; i++)

{

int key = arr[i];

int j = i - 1;

// compare to all predecessors

while (j >= 0 && arr[j] > key)

{

arr[j + 1] = arr[j];

j = j - 1;

}

arr[j + 1] = key;

}

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << " ";

cout << endl;

}

int main()

{

// int arr[] = {64, 34, 25, 12, 22, 11, 90};

// int n = sizeof(arr)/sizeof(arr[0]);

int n = rand() % 100;

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

cout << "Array: ";

printArray(arr, n);

cout << endl;

auto start = chrono::high\_resolution\_clock::now();

// unsync the I/O of C and C++.

ios\_base::sync\_with\_stdio(false);

insertionSort(arr, n);

auto end = chrono::high\_resolution\_clock::now();

cout << "Sorted array: ";

printArray(arr, n);

cout << endl;

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

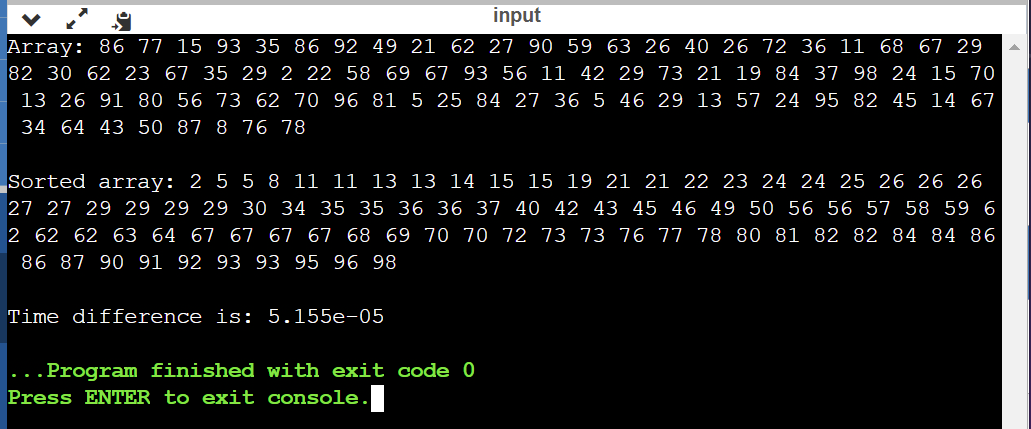
time\_taken \*= 1e-9;

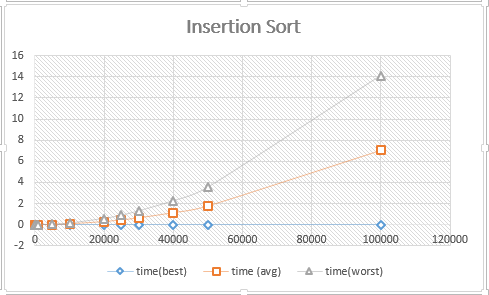
cout << "Time difference is: " << time\_taken << setprecision(6);

return 0;

}

**Output:**





# Batch Analysis:

**Source Code:**

#include <bits/stdc++.h>

#include <chrono>

using namespace std;

// place current element in right order as we move forward

void insertionSort(int arr[], int n)

{

for (int i = 1; i < n; i++)

{

int key = arr[i];

int j = i - 1;

// compare to all predecessors

while (j >= 0 && arr[j] > key)

{

arr[j + 1] = arr[j];

j = j - 1;

}

arr[j + 1] = key;

}

}

void printArray(double arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(int arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

void printArray(float arr[], int size)

{

for (int i = 0; i < size; i++)

cout << arr[i] << ", ";

cout << endl;

}

double sortApp(int n)

{

int arr[n];

for (int i = 0; i < n; i++)

{

arr[i] = rand() % 100;

}

auto start = chrono::high\_resolution\_clock::now();

ios\_base::sync\_with\_stdio(false);

insertionSort(arr, n);

auto end = chrono::high\_resolution\_clock::now();

double time\_taken = chrono::duration\_cast<chrono::nanoseconds>(end - start).count();

time\_taken \*= 1e-9;

return time\_taken;

}

int main()

{

double times[10];

int ns[10];

for (int x = 0; x < 10; x++)

{

int n = rand() % 100;

ns[x] = n;

times[x] = sortApp(n);

}

cout << "value of n's: " << endl;

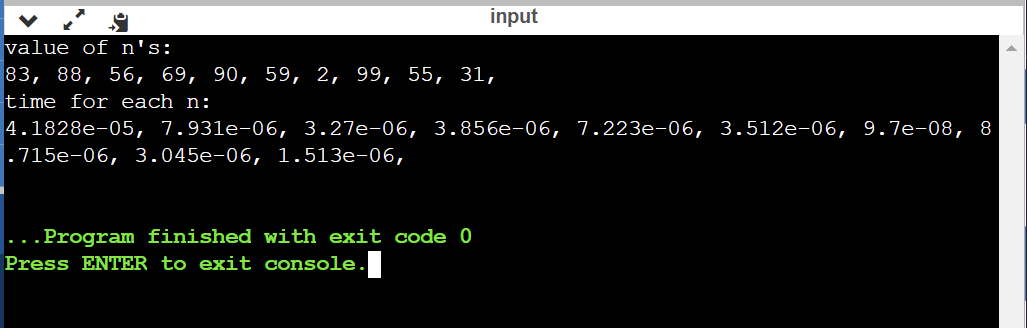
printArray(ns, 10);

cout << "time for each n: " << endl;

printArray(times, 10);

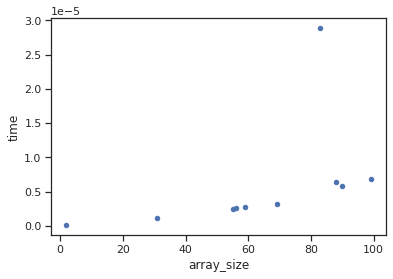
}

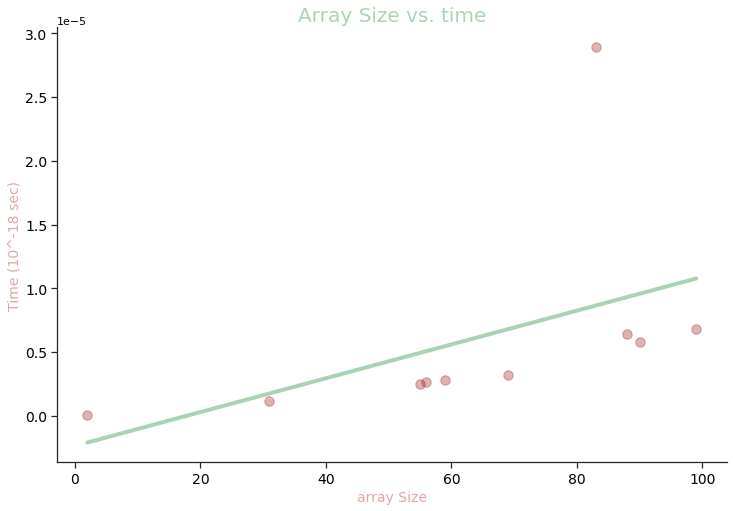
**Output:**



**arraySize = [83, 88, 56, 69, 90, 59, 2, 99, 55, 31]**

**time = [2.8917e-05, 6.425e-06, 2.608e-06, 3.153e-06, 5.76e-06, 2.767e-06, 5.5e-08, 6.81e-06, 2.451e-06, 1.186e-06]**

****

****

**Insertion Sort**

# **Viva Questions**

### **1. Why is time complexity of insertion sort?**

### Ans.

Even though insertion sort is efficient, still, if we provide an already sorted array to the insertion sort algorithm, it will still execute the outer for loop, thereby requiring n steps to sort an already sorted array of n elements, which makes its best case time complexity a linear function of n.

Wherein for an unsorted array, it takes for an element to compare with all the other elements which mean every n element compared with all other n elements. Thus, making it for n x n, i.e., n2 comparisons. One can also take a look at other sorting algorithms such as *Merge sort, Quick Sort, Selection Sort*, etc. and understand their complexities.

**Worst Case Time Complexity [ Big-O ]: O(n2)**

**Best Case Time Complexity [Big-omega]: O(n)**

**Average Time Complexity [Big-theta]: O(n2)**

### **2. Is it possible to do insertion sort in place?**

Ans.

Yes, It is. Insertion sort is used when number of elements is small. It can also be useful when input array is almost sorted, only few elements are misplaced in complete big array.

### **3. Is insertion sort the worst?**

Ans.

nsertion sort has a fast best-case running time and is a good sorting algorithm to use if the input list is already mostly sorted. For larger or more unordered lists, an algorithm with a **faster worst** and average-case running time, such as mergesort, would be a better choice. Now iterate through this array just one time.The time

### **4. What is Binary Insertion Sort?**

Ans.

We can use binary search to reduce the number of comparisons in normal insertion sort. Binary Insertion Sort uses binary search to find the proper location to insert the selected item at each iteration. In normal insertion, sorting takes O(i) (at ith iteration) in worst case. We can reduce it to O(logi) by using binary search. The algorithm, as a whole, still has a running worst case running time of O(n^2) because of the series of swaps required for each insertion.

### **5. Is insertion sort stable and in-place?**

Ans.

Insertion sort is an online stable in-place sorting algorithm that builds the final sorted list one item at a time. It works on the principle of moving a element to its correct position in a sorted array. Advantages of Insertion Sort: Stable: it does not change the relative order of elements with equal keys.

### **6. Give any application of insertion sort?**

Ans.

Insertion sort is used when number of elements is small. It can also be useful when input array is almost sorted, only few elements are misplaced in complete big array.